

# Bled'11 - 7th Slovenian International Conference on Graph Theory

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## k-restricted edge-connectivity in triangle-free graphs

### Content :

Let  $G$  be a  $\lambda_k$ -connected graph.  $G$  is called  $\lambda_k$ -optimal, if its  $k$ -restricted edge-connectivity  $\lambda_k(G)$  equals its minimum  $k$ -edge degree.  $G$  is called super- $\lambda_k$  if every  $\lambda_k$ -cut isolates a connected subgraph of order  $k$ .

Firstly, we will introduce a lower bound on the order of  $2$ -fragments in triangle-free graphs that are not  $\lambda_2$ -optimal. Secondly, we present an Ore-type condition for triangle-free graphs to be  $\lambda_3$ -optimal. Thirdly, we prove a lower bound on the order of  $k$ -fragments in triangle-free  $\lambda_k$ -connected graphs, and use it to show that triangle-free graphs with high minimum degree are  $\lambda_k$ -optimal and super- $\lambda_k$ .

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